

CLAIMS

1. A method of universal calculation on points on  
5 an elliptic curve, characterised in that the elliptic  
curve is defined by a quartic equation and in that  
identical programmed calculation means are used to  
carry out an operation of addition of points, an  
operation of doubling of points, and an operation of  
10 addition of a neutral point, the calculation means  
comprising in particular a central processing unit (2)  
associated with a memory (4, 6, 8).

2. A method according to Claim 1, characterised  
15 in that the elliptic curve is defined by a quartic  
equation of the type:

$$V^2 = b \cdot U^4 + a \cdot U^3W + UW^3,$$

20 (U : V : W) being Jacobi projective coordinates  
of a point P on the elliptic curve, and a, b being  
parameters of the elliptic curve, a point with  
coordinates (0 : 0 : 1) being a neutral point O of the  
elliptic curve, a point with coordinates (U : -V : W)  
25 being an inverse point (-P) of the point P with  
coordinates (U : V : W).

3. A method according to Claim 2, in which the  
point P is also defined in affine coordinates (X, Y),  
30 the affine coordinates (X, Y) and the Jacobi projective

coordinates  $(U : V : W)$  of the point  $P$  being linked by the relationships:

$$(X, Y) = (U/W, V/W^2).$$

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4. A method according to Claim 2 or 3, in which, in order to carry out the addition of a first point  $P_1$  defined by first Jacobi projective coordinates  $(U_1 : V_1 : W_1)$  and a second point  $P_2$  defined by second Jacobi projective coordinates  $(U_2 : V_2 : W_2)$ , the coordinates of the first point  $P_1$  and those of the second point  $P_2$  being stored in first and second registers in the memory (4, 6, 8), the first point and the second point belonging to the elliptic curve,

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the programmed calculation means calculate third Jacobi projective coordinates  $(U_3 : V_3 : W_3)$  defining a third point  $P_3$ , the result of the addition, by the following equations:

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$$\begin{aligned} U_3 = & 2.b.U_1^2.U_2^2 \\ & + (aU_1.U_2 + W_1.W_2).(U_1.W_2+W_1.U_2) + \end{aligned}$$

$2V_1.V_2$

25

$$\begin{aligned} V_3 = & (U_1^2.V_2+U_2^2.V_1)* \\ & (4b.(U_1.W_2+U_2.W_1).W_1.W_2 \\ & - 8b^2.(U_1.U_2)^2 \\ & + a.[(2W_1.W_2)^2 - (aU_1.U_2+W_1.W_2)^2] \\ & + (W_1^2.V_2+W_2^2.V_1)* \end{aligned}$$

$$\begin{aligned}
 & [(aU_1.U_2 + W_1.W_2)^2 - (2aU_1.U_2)^2] \\
 & 4bU_1.U_2.(W_1.U_2 + U_1.W_2) \\
 & - 4bU_1.U_2.(U_1.W_1.V_2 + U_2.W_2.V_1)(aU_1.U_2 - W_1.W_2)
 \end{aligned}$$

5             $W_3 = (aU_1.U_2 - W_1.W_2)^2 - 4bU_1.U_2(U_1.W_2 + U_2.W_1)$

and then store the third projective coordinates  
 $(U_3 : V_3 : W_3)$  in third registers in the memory (6, 8).

10            5. A method according to Claim 1, in which the elliptic curve is a curve comprising a single point of order two and is defined by a quartic equation of the type:

15             $V^2 = \varepsilon.U^4 - 2\delta.U^2.W^2 + W^4,$

20             $(U : V : W)$  being Jacobi projective coordinates of a point  $P$  on the elliptic curve, and  $\varepsilon, \delta$  being parameters of the elliptic curve, the point with coordinates  $(0 : 1 : 1)$  being the neutral point  $O$  of the elliptic curve, the point with coordinates  $(-U : +V : W)$  being the inverse point  $(-P)$  of the point  $P$  ( $U : V : W$ ).

25            6. A method according to Claim 5, in which, in order to carry out the addition of the first point  $P_1$  defined by first Jacobi projective coordinates  $(U_1 : V_1 : W_1)$  and the second point  $P_2$  defined by second Jacobi projective coordinates  $(U_2 : V_2 : W_2)$ , the coordinates 30 of the first point  $P_1$  and those of the second point  $P_2$

being stored in first and second registers in the memory (4, 6, 8), the first point and the second point belonging to the elliptic curve,

5 the programmed calculation means calculate third Jacobi projective coordinates ( $U_3 : V_3 : W_3$ ) defining a third point  $P_3$ , the result of the addition, by the following equations:

10  $U_3 = U_1 \cdot W_1 \cdot V_2 + V_1 \cdot U_2 \cdot W_2$

$$V_3 = [(W_1 \cdot W_2)^2 + \epsilon(U_1 \cdot U_2)^2] \\ * [V_1 \cdot V_2 - \\ 2\delta U_1 \cdot U_2 \cdot W_1 \cdot W_2] + 2\epsilon \cdot U_1 \cdot U_2 \cdot W_1 \cdot W_2 (U_1^2 W_2^2 + W_1^2 U_2^2)$$

15  $W_3 = (W_1 \cdot W_2)^2 - \epsilon(U_1 \cdot U_2)^2$

and then store the third projective coordinates ( $U_3 : V_3 : W_3$ ) in the third registers in the memory (6, 20 8).

7. A method according to one of Claims 5 to 6, in which the elliptic curve is defined in affine coordinates by an equation of the type:

25  $Y^2 = \epsilon \cdot X^4 - 2\delta \cdot X^2 + 1$

$(X, Y)$  being affine coordinates of a point  $P$  on the elliptic curve.

8. A method according to Claim 7, in which, in  
 order to carry out the addition of the first point P1  
 defined by first affine coordinates (X1, Y1) and the  
 5 second point P2 defined by second affine coordinates  
 (X2, Y2), the coordinates of the first point P1 and  
 those of the second point P2 being stored in first and  
 second registers in the memory (4, 6, 8), the first  
 point P1 and the second point P2 belonging to the  
 10 elliptic curve,

the programmed calculation means calculate third  
 affine coordinates (X3, Y3) defining a third point P3,  
 the result of the addition, by the following equations:

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$$X3 = (X1.Y2 + Y1.X2) / [1 - \epsilon(X1.X2)^2]$$

$$Y3 = \frac{\{[1+\epsilon(X1.X2)^2] \cdot [Y1.Y2 - 2\delta.X1.X2] + 2\epsilon.X1.X2.(X1^2+X2^2)\}}{[1 - \epsilon(X1.X2)^2]}$$

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and then store the third affine coordinates (X3, Y3) in the third registers in the memory (6, 8).

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9. A method according to one of Claims 5 to 8, in  
 which the elliptic curve is a curve comprising three  
 points of order two and has  $\epsilon = 1$  as a parameter.

10. Use of a calculation method according to one of Claims 1 to 9 in a scalar multiplication calculation method applied to points on an elliptic curve.

5           11. Use of a calculation method according to one of Claims 1 to 9 in a cryptographic method.

10          12. An electronic component comprising programmed calculation means for implementing a method according to one of Claims 1 to 9, the calculation means comprising in particular a central processing unit (2) associated with a memory (4, 6, 8).

15          13. An electronic component comprising means for implementing a cryptographic algorithm using a method according to one of Claims 1 to 9.

14. A smart card comprising an electronic component according to Claim 12 or 13.